MARK SCHEME
Maximum Mark: 120

## Published

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge International will not enter into discussions about these mark schemes.
Cambridge International is publishing the mark schemes for the October/November 2019 series for most Cambridge IGCSE ${ }^{\text {TM }}$, Cambridge International A and AS Level components and some Cambridge O Level components.

## Generic Marking Principles

These general marking principles must be applied by all examiners when marking candidate answers. They should be applied alongside the specific content of the mark scheme or generic level descriptors for a question. Each question paper and mark scheme will also comply with these marking principles.

## GENERIC MARKING PRINCIPLE 1:

Marks must be awarded in line with:

- the specific content of the mark scheme or the generic level descriptors for the question
- the specific skills defined in the mark scheme or in the generic level descriptors for the question
- the standard of response required by a candidate as exemplified by the standardisation scripts.

GENERIC MARKING PRINCIPLE 2:
Marks awarded are always whole marks (not half marks, or other fractions).

## GENERIC MARKING PRINCIPLE 3:

Marks must be awarded positively:

- marks are awarded for correct/valid answers, as defined in the mark scheme. However, credit is given for valid answers which go beyond the scope of the syllabus and mark scheme, referring to your Team Leader as appropriate
- marks are awarded when candidates clearly demonstrate what they know and can do
- marks are not deducted for errors
- marks are not deducted for omissions
- answers should only be judged on the quality of spelling, punctuation and grammar when these features are specifically assessed by the question as indicated by the mark scheme. The meaning, however, should be unambiguous.

GENERIC MARKING PRINCIPLE 4:
Rules must be applied consistently e.g. in situations where candidates have not followed instructions or in the application of generic level descriptors.

## GENERIC MARKING PRINCIPLE 5:

Marks should be awarded using the full range of marks defined in the mark scheme for the question (however; the use of the full mark range may be limited according to the quality of the candidate responses seen).

GENERIC MARKING PRINCIPLE 6:
Marks awarded are based solely on the requirements as defined in the mark scheme. Marks should not be awarded with grade thresholds or grade descriptors in mind.

## MARK SCHEME NOTES

The following notes are intended to aid interpretation of mark schemes in general, but individual mark schemes may include marks awarded for specific reasons outside the scope of these notes.

## Types of mark

M Method marks, awarded for a valid method applied to the problem.
A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. For accuracy marks to be given, the associated Method mark must be earned or implied.

B Mark for a correct result or statement independent of Method marks.
When a part of a question has two or more 'method' steps, the M marks are in principle independent unless the scheme specifically says otherwise; and similarly where there are several B marks allocated. The notation 'dep' is used to indicate that a particular $M$ or $B$ mark is dependent on an earlier mark in the scheme.

## Abbreviations

awrt answers which round to
cao correct answer only
dep dependent
FT follow through after error
isw ignore subsequent working
nfww not from wrong working
oe or equivalent
rot rounded or truncated
SC Special Case
soi seen or implied

| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 1(a) | Correct triangle with vertices $(3,-5),(5,-5),(5,-4)$ | 1 |  |
| 1(b) | Correct triangle with vertices $(3,2),(5,2),(5,1)$ | 1 |  |
| 1(c) | Reflection $y=-1.5 \mathrm{oe}$ | 2 | B1 for each |
| 1(d) | Correct triangle with vertices $(-5,3),(-5,5),(-4,5)$ | 2 | B1 for correct rotation with incorrect centre of rotation. <br> or B1 for clockwise rotation with correct centre of rotation. |
| 1(e) | Reflection $y=x \mathrm{oe}$ | 2 | B1 for each |
| 2(a) | 0.25 oe | 1 |  |
| 2(b) | 1.5 | 2 | M1 for $1=-2(x-2)$ or $\frac{1}{-2}=x-2$ |
| 2(c) | $(x+2)^{2}$ | 1 |  |
| 2(d) | $-0.5 \text { or }-\frac{1}{2}$ | 4 | B1 for $x^{2}+4 x+4$ <br> M2 for $4 x+4=2$ or M1 for their $(c)=x^{2}+2$ <br> or <br> M2 for correct sketch or M1 for any U-shaped parabola |
| 2(e) | $\frac{1}{x}+2$ oe final answer | 3 | M2 for $x=\frac{1}{y}+2$ or $x y=1+2 y$ or $y-2=\frac{1}{x}$ or M1 for $x-2=\frac{1}{y}$ or $y(x-2)=1$ or $x=\frac{1}{y-2}$ |
| 2(f)(i) |  | 3 | B1 for correct quadratic shape through origin <br> B2 for correct rectangular hyperbola shape or B1 for one branch |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 2(f)(ii) | $x=0$ | 1 |  |
| 2(f)(iii) | $2<x<2.21$ or 2.205 to 2.206 | 2 | B1 for each part or 2 and 2.21 or 2.205 to 2.206 seen |
| 3(a) | $160 \times \frac{4}{5} \text { oe }$ | 1 |  |
| 3(b) | 57.60 | 3 | M2 for $128 \times \frac{4}{5}$ or $\frac{160-x}{128}=\frac{4}{5}$ or M1 for $\frac{128}{5}$ or $\frac{160-x}{4}$ or $160-x: 128=4: 5$ |
| 3(c)(i) | 25 | 1 |  |
| 3(c)(ii) | 40 | 3 | M2 for $32 \times \frac{100}{80}$ oe or M1 equating 32 to $80 \%$ |
| 4(a)(i) | -4 | 2 | M1 for $2 x=-11+3$ or $x-\frac{3}{2}=\frac{11}{2}$ oe |
| 4(a)(ii) | -9 | 2 | M1 for $36=-4 x$ or $\frac{36}{-4}=x$ oe |
| 4(a)(iii) | 0.5 oe | 2 | M1 for $6 x+2 x=17-13$ oe |
| 4(b) | Correctly equating one set of coefficients <br> OR <br> $x=\ldots$ or $y=\ldots$ from one equation | M1 | Allow correct sketches, i.e. two lines with negative gradients |
|  | Correct method for eliminating one variable <br> OR correct substitution into other equation | M1 |  |
|  | $\begin{aligned} & {[x=]-2} \\ & {[y=]-3} \end{aligned}$ | B2 | B1 for each <br> If 0 scored, $\mathbf{S C 1}$ for correct substitution in one of the original equations to find other variable |
| 5(a)(i) | 140 | 2 | B1 for angle $O B A=20$ soi |
| 5(a)(ii) | 70 | 1 | FT $0.5 \times$ their (i) |
| 5(a)(iii) | 110 | 1 | FT 180-their(ii) |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 5(a)(iv) | 45 | 1 |  |
| 5(a) (v) | 25 | 1 |  |
| 5(a)(vi) | 40 | 1 |  |
| 5(b) | Cyclic [quadrilateral] | 1 |  |
| 6(a) | 0 cao | 1 |  |
| 6(b) | $\frac{5}{6} \text { oe }$ | 1 |  |
| 6(c) | $\frac{4}{24} \text { oe }$ | 2 | M1 for $\frac{1}{4} \times \frac{1}{6}$ or B1 for $\frac{k}{24}$ soi $k$ integer from 1 to 23 |
| 6(d) | $\frac{12}{24} \text { oe }$ | 3 | M2 for $\frac{2}{4} \times \frac{3}{6}+\frac{2}{4} \times \frac{3}{6}$ oe or for 12 pairs listed or indicated or M1 for $\frac{2}{4} \times \frac{3}{6}$ oe or for 10 or 11 pairs listed or indicated |
| 6(e) | $\frac{4}{24} \text { oe }$ | 2 | M1 for $\frac{1}{4} \times \frac{1}{6}$ or for $(1,5)(2,4)(3,3)(4,2)$ listed or indicated |
| 7(a)(i) | $(2 x+1)(x-6)$ final answer | 2 | $\begin{aligned} & \text { M1 for }(2 x+a)(x+b) \text { where } \\ & a b=-6 \text { or } a+2 b=-11 \\ & \text { or } 2 x(x-6)+x-6 \text { or } x(2 x+1)-6(2 x+1) \end{aligned}$ or correct answer seen |
| 7(a)(ii) | $-0.5<x<6$ | 2 | FT their (i) only from factors giving positive $x^{2}$ term <br> B1 for each or -0.5 and 6 seen |
| 7(b) | Appropriate sketch indicating answers (one positive and one negative) or correct substitution in formula or correct completion of square | M1 | Allow $\sqrt{61}$ for $\sqrt{(-1)^{2}-4(3)(-5)}$ |
|  | $\begin{aligned} & 1.47 \\ & -1.14 \end{aligned}$ | B2 | B1 for each or both correct but not rounded to 2dp 1.468... ,-1.135... |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 8(a) | Correct Venn diagram | 2 | B1 for $2,4,12,18$ correct <br> B1 for $y$ and $56-y$ correct oe |
| 8(b)(i) | 8 | 2 | M1 for $100=74+18+x$ oe |
| 8(b)(ii) | 40 | 2 | M1 for $16+\operatorname{their}(x)+y=2(24+\operatorname{their}(x))$ oe |
| 8(b)(iii) | 16 | 1 | FT 56 - their (b)(ii) (their (b)(ii) $\leqslant 56)$ |
| 9(a) | $[(14 \times 18)+0.5 \times 14 \times 8] \times 24 \text { oe }$ or $18 \times 14 \times 24+0.5 \times 14 \times 8 \times 24$ oe leading to 7392 | M3 | i.e. area $\times$ length <br> volume + volume <br> M2 for $14 \times 18+0.5 \times 14 \times 8$ <br> or M1 for $14 \times 18$ or $0.5 \times 14 \times 8$ or $0.5 \times(18+26) \times 7$ |
| 9(b) | 12 cao | 3 | M2 for $24 \div \sqrt[3]{\frac{7392}{924}}$ oe or M1 for $\sqrt[3]{\frac{7392}{924}}$ soi |
| 9(c) | 12.1 or $2.08 \ldots$ | 2 | M1 for $r^{3}=\frac{3}{4} \times \frac{7392}{\pi}$ oe |
| 9(d) | 48.2 or 48.3 or 48.4 or 48.20 to 48.37 ... | 2 | M1 for $h=\frac{3 \times 7392}{\pi \times(\text { their } 12.1)^{2}}$ |
| 9(e) | $\pi r^{2} \sqrt{17}$ final answer | 3 | M2 for $\pi r \sqrt{r^{2}+(4 r)^{2}}$ or M1 for $l^{2}=r^{2}+(4 r)^{2}$ If 0 scored, $\mathbf{S C 1}$ for $\pi r^{2} \sqrt{5}$ |
| 10(a) | 129.25 | 2 | M1 for at least 3 of 50, 110, 130, 150, 205 seen |
| 10(b) | $140[<m \leqslant] 160$ | 1 |  |
| 10(c) | $\frac{189}{1580}$ | 3 | B2 for $0.12[0]$ or $0.1196 \ldots$ or $\frac{756}{6320}$ oe or M1 for $\frac{28}{80} \times \frac{27}{79}$ |


| Question | Answer | Marks | Partial Marks |
| :---: | :---: | :---: | :---: |
| 10(d)(i) | $0.06,1.1,1.55,0.65,0.0889$ or 0.08888 to 0.08889 | 2 | B1 for 3 or 4 correct |
| 10(d)(ii) | Correct histogram | 3 | B1 for correct widths B2 FT for all heights correct or B1 FT for 3 or 4 correct heights |
| 11(a) | $8^{2}+9^{2}-2 \times 8 \times 9 \times \cos 64$ | M1 |  |
|  | $9.048 \ldots$ [ $\quad$ 9.05] | A1 |  |
| 11(b)(i) | [Area $A B D]=0.5 \times 8 \times 9 \times \sin 64$ | M1 |  |
|  | Area $B D C=57.3-$ their $A B D$ | M1 |  |
|  | their $24.94=0.5 \times 6.5 \times 9.05 \times \sin B D C$ | M1 |  |
|  | Angle $B D C=57.98$ to 58.02 | A1 | If 58.0... must see 58.0 not 58 alone |
| 11(b)(ii) | 77.4 to $77.54 \ldots$ | 5 | M1 for $6.5^{2}+9.05^{2}-2 \times 6.5 \times 9.05 \times \cos 58$ <br> A2 for $\sqrt{61.8}$ or 7.86 <br> or A1 for 61.8 seen <br> M1 for $\frac{\text { their } 7.86}{\sin 58}=\frac{9.05}{\sin B C D}$ oe <br> or $\frac{1}{2} \times$ their $7.86 \times 6.5 \times \sin B C D=$ their 24.94 or $9.05^{2}=6.5^{2}+(\text { their } 7.86)^{2}-$ <br> $2 \times 6.5 \times($ their 7.86$) \times \cos B C D$ or better |
| 12(a) |  | 4 | B1 for each branch |
| 12(b) | $\begin{aligned} & x=0 \\ & x=1 \\ & x=-1 \\ & y=0 \end{aligned}$ | 3 | B2 for three correct or B1 for one correct |
| 12(c) | $\begin{aligned} & (0.577,-2.6[0]) \\ & \text { or }(0.5773 \text { to } 0.5774,-2.598 \ldots) \end{aligned}$ | 2 | B1 for each |
| 12(d) | $\begin{aligned} & {[x=]-1.24 \quad \text { or }-1.242 \text { to }-1.241} \\ & {[x=] 1.13 \text { or } 1.127 \text { to } 1.128} \end{aligned}$ | 2 | B1 for each |

